

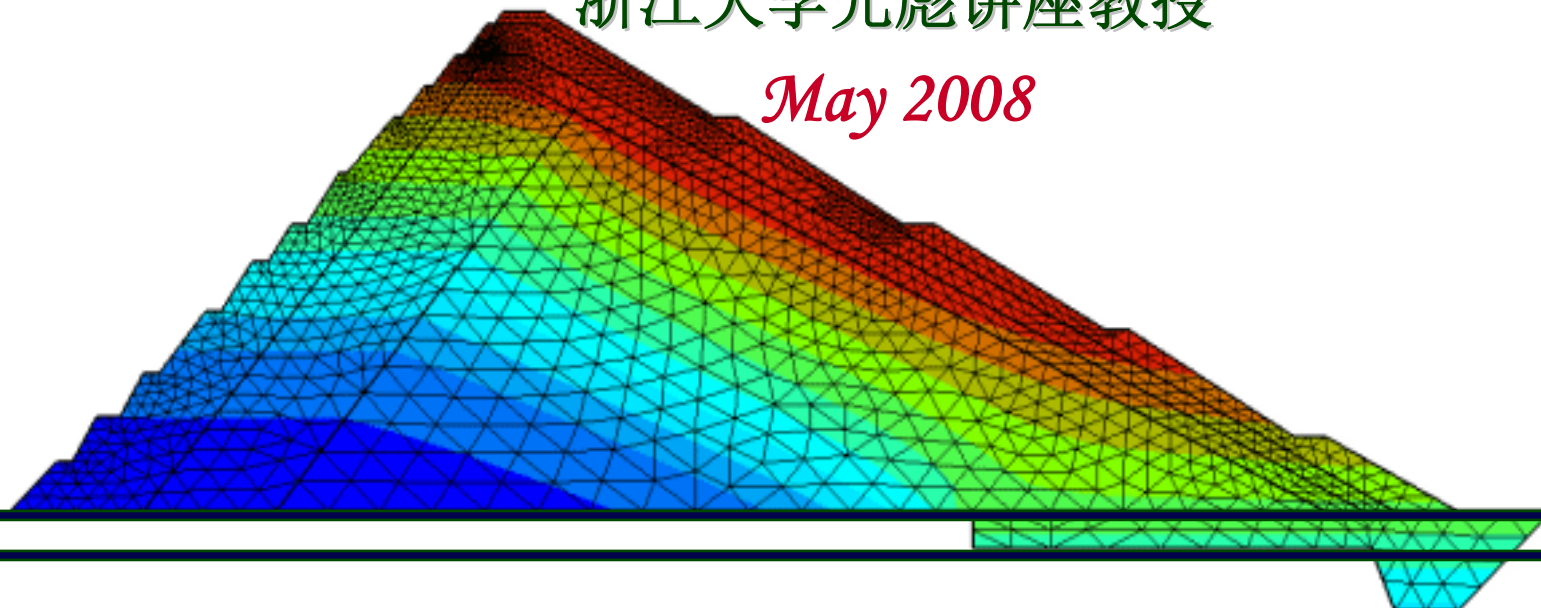
# ***Teaching Soil Mechanics (Civil Engineering) at University in the Years 2000+***

二十一世纪大学土力学的教学（土木工程）

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*May 2008*



## *Common Complaints from Students about Soil Mechanics* 学生们的抱怨

- ***Soil Mechanics concepts are quite difficult to assimilate with the study of other materials***  
土力学的概念难以与其他材料学科融会贯通

## *Common Complaints after Graduation about Soil Mechanics* 学生毕业后的抱怨

- ***Soil Mechanics taught at university is quite removed from the practice of Geotechnical Engineering***  
大学里教授的土力学脱离工程实践

*Soil Mechanics is a Young Science;  
Starting in the 1930s*

土力学是一门年轻的学科，始于二十世纪三十年代

- **Focus on** 关注点：

- *Impact of the computer on how we **practice** Soil Mechanics*

计算机对实践土力学的意义

- *Impact of the computer on how we **teach** Soil Mechanics*

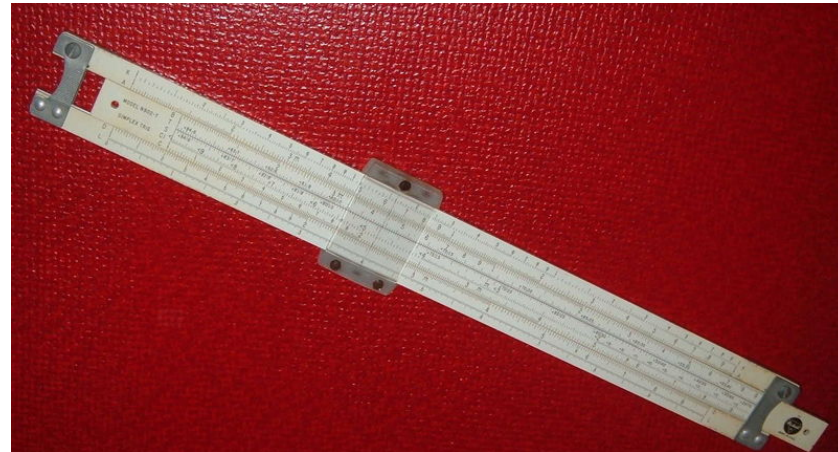
计算机对讲授土力学的意义

# *How did engineers perform calculations prior to the invention of the digital computer?*

在电脑发明以前，工程师们如何进行计算？



**Engineer in the 1970s**  
二十世纪七十年代的工程师



**Slide Rule for multiplication, division, log & trig functions, etc.**

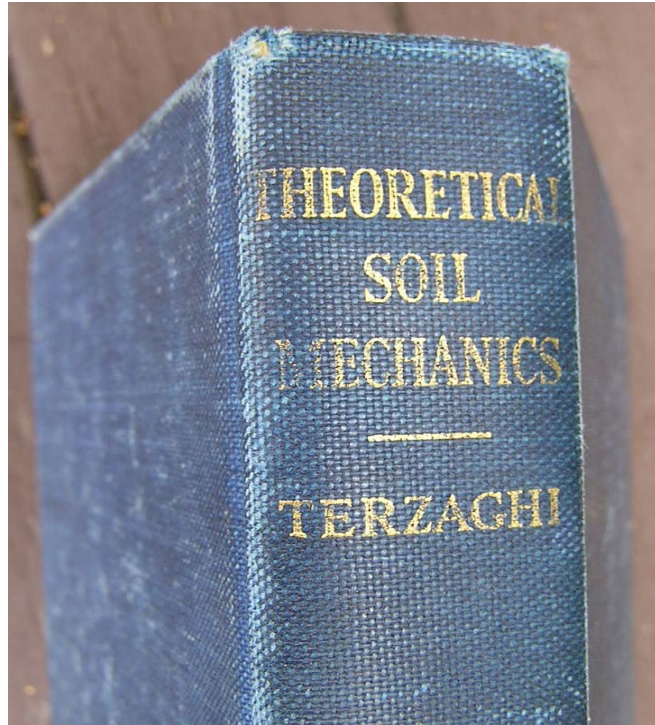
计算尺：用于乘法、除法、对数和三角运算等





# *Birth of Saturated Soil Mechanics*

## 饱和土力学的诞生



- **1943 Karl Terzaghi wrote “Theoretical Soil Mechanics”**  
1943年，太沙基写出《理论土力学》
- **Saturated soil behavior is controlled by the effective stress variable,  $(\sigma - u_w)$**   
有效应力 $(\sigma - u_w)$ 决定饱和土的性质

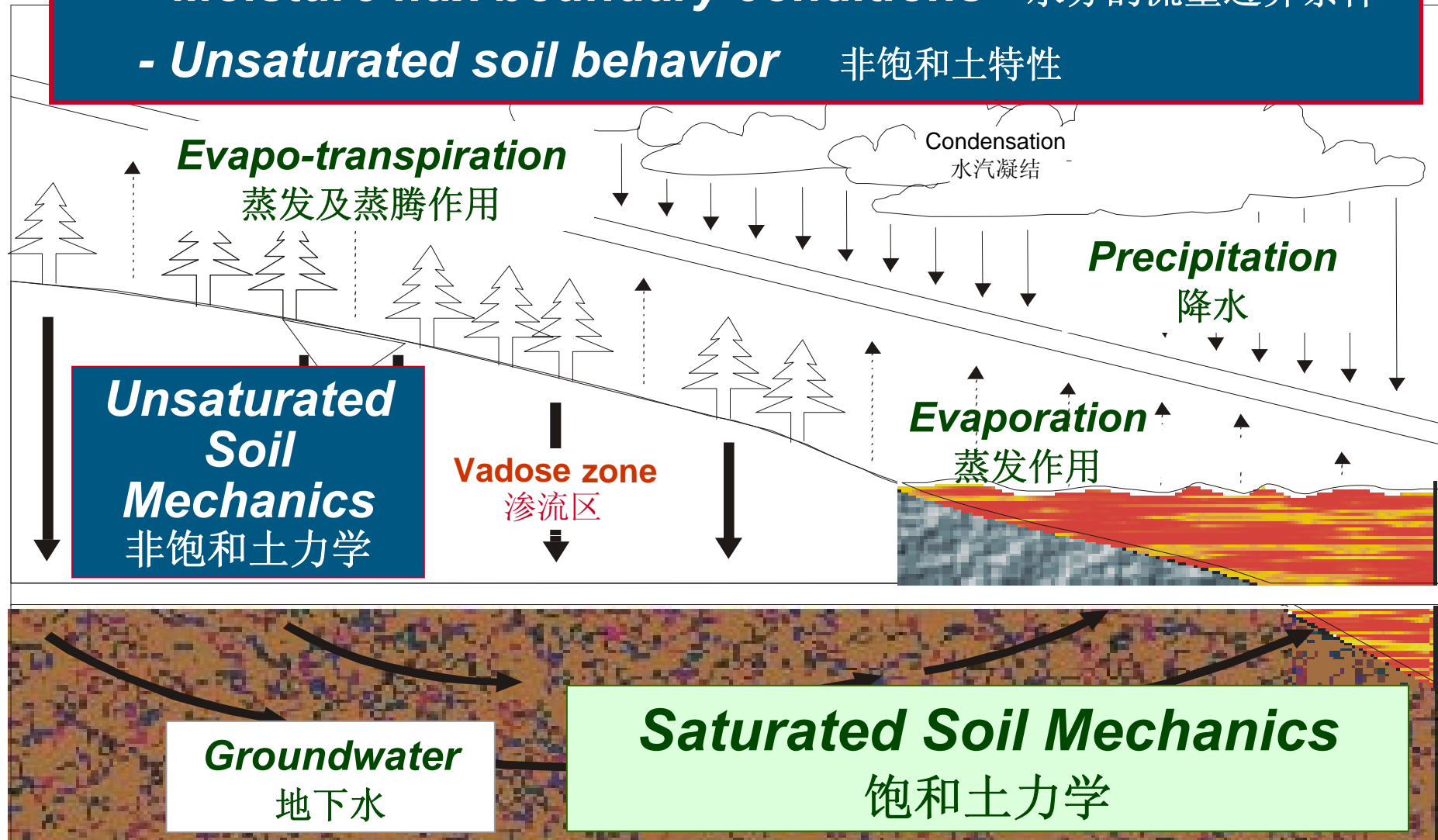
**Attempt was to make *Soil Mechanics* a science with *closed-form solutions* for simplified representations of geotechnical problems**

试图利用地质学问题中有**闭合解**的简单表达式使**土力学**成为一门科学

# *Classical Soil Mechanics developed without:*

经典土力学的发展没有包括

- **Moisture flux boundary conditions** 水分的流量边界条件
- **Unsaturated soil behavior** 非饱和土特性

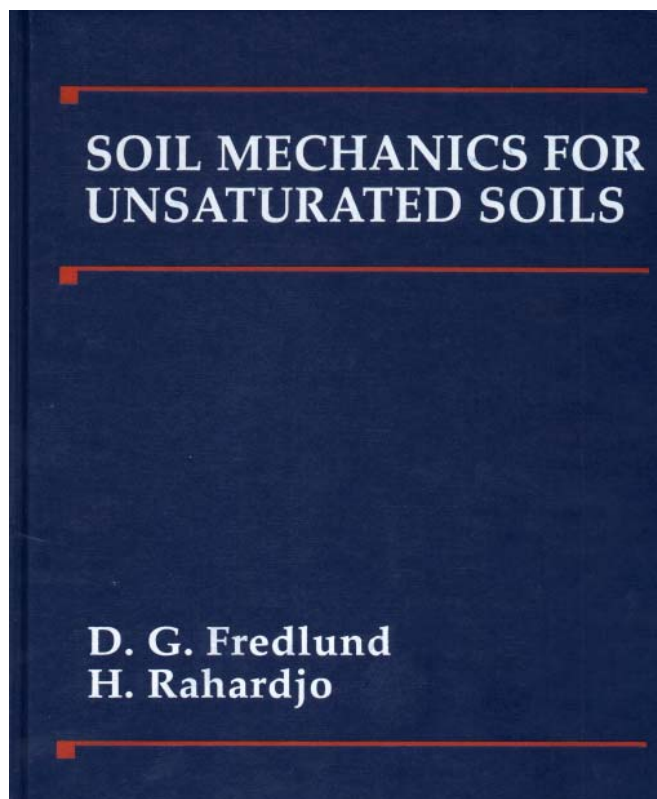


# *Evolution of Unsaturated Soil Mechanics*

## 非饱和土力学的进展

- **1970s Unsaturated Soil behavior is controlled by two stress variables; namely, net total stress,  $(\sigma - u_a)$ , and matric suction,  $(u_a - u_w)$**

二十世纪七十年代，非饱和土特性由两个应力参数决定，即：净总应力（ $\sigma - u_a$ ）和基质吸力（ $u_a - u_w$ ）



**Attempt was to make  
*Unsaturated Soil Mechanics* a  
science through use of  
*boundary-value  
representations of saturated-  
unsaturated soil problems***

试图通过使用饱和—非饱和土问题的边界值  
表达式使非饱和土力学成为一门科学

***Computers influence how a science  
is presented and practiced***

# *Impact of Computers on Geotechnical Engineering*

## 计算机对岩土工程的影响

- ❑ ***Field Logging*** soil observations can be entered electronically in the field  
现场记录 观测结果可以在现场进行电子输入
- ❑ ***Laboratory test*** data can be entered into a database and calculations performed  
室内实验 数据可以输入数据库进行计算
- ❑ ***Spreadsheets*** (e.g., EXCEL) are used for simple calculations and simple problem solving  
电子表格(如Excel) 可用于简单的计算和解决问题
- ❑ ***Word Processors*** are used for writing reports  
文字处理软件 可用于报告写作



# *Impact of Computers on Geotechnical Engineering*

## 计算机对岩土工程的影响

- ❑ **Graphics Software is used to prepare plots and figures**  
图形处理软件 用于绘制图表
- ❑ **Knowledge-based database used to store and retrieve past experience and estimate soil properties** 知识库 用于查询实例，估测土性及土性函数
- ❑ **Numerical modeling software is used to solve a wide variety of Soil Mechanics problems** 数值模拟 可以解决很多土力学中的问题
- ❑ **PowerPoint and other software used to communicate with clients and agencies. Professors also use PowerPoint at University.** PowerPoint等 软件可用于技术交流和教学

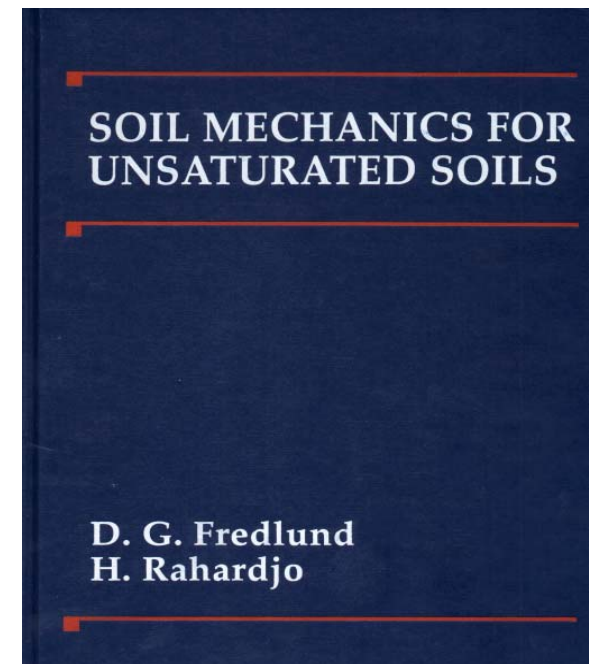
**All Software Packages should be Transparent**

所有软件都必须是“透明”的

# Objectives of a Soil Mechanics Course

## 土力学的课程目标

- **Teach Soil Behavior and Problem Solving**  
(e.g., seepage, shear strength, volume change)  
讲授土的性状，解决土的问题(如：渗流，抗剪强度和体变)，包括
  - **Theory associated with Constitutive behavior**  
与本构关系相关的理论
  - **Measurement of the soil properties**  
土性测量
  - **Estimation of the soil properties**  
土性预测
  - **Application of theory in the form of a formulation of the practical engineering problem**  
应用理论解决实际问题



# *Geotechnical Engineering Practice is about Predicting the Future*

岩土工程就是做预测！

*Predictions may be difficult for several reasons:*

- ***The physics of the model may not be sufficiently rigorous***  
物理模型不够严格
- ***The input soil properties may not be sufficiently known or assessed***  
土性参数不够精确
- ***The initial conditions and boundary conditions may not be sufficiently defined***  
初始条件和边界条件不足于确定
- ***The computer results might not be properly interpreted***  
对电算结果不能给予准确的解释

*It is extremely  
difficult to  
predict the  
future but if we  
do not attempt  
to do so, we will  
live without a  
“Vision for  
Survival”*

尽管困难，  
但若不做预测，  
就无法“预见生机”

# OOPS...DID I SAY THAT?

Forecasting the future is a fool's game, especially when it comes to technology.

**“640K OUGHT TO BE  
ENOUGH FOR ANYBODY.”**

—BILL GATES,  
founder of Microsoft, 1981

**“I THINK THERE IS A WORLD  
MARKET FOR MAYBE FIVE  
COMPUTERS.”**

—THOMAS WATSON JR.,  
chairman of IBM, 1943

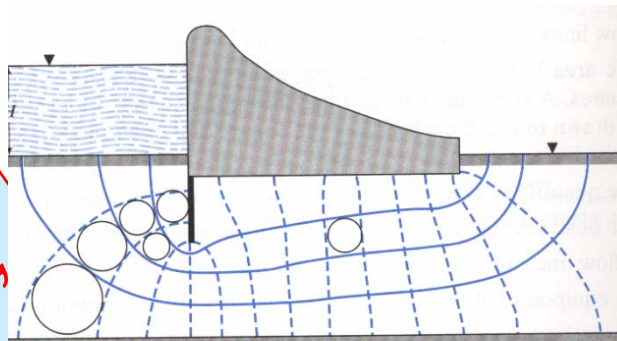


旧的模式：只要能挣钱，为什么要改变？

**Focus of the Past**

**“If we’re making money,  
why change?”**

**The Old Paradigm**

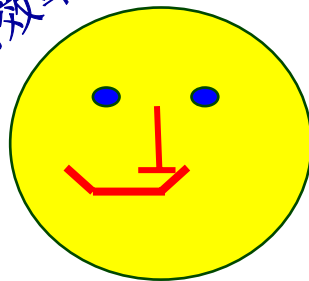


**The New Paradigm**

**Focus of the Future**

**“Can our efficiency and  
effectiveness be improved?”**

新的模式：提高效率 and 有效性！

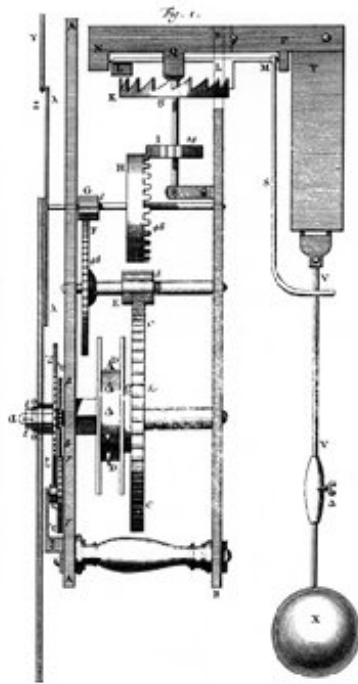




# *What is a Paradigm Shift?*

## 什么是“观念上的转变”？

***Clock with Moving Parts***  
带钟摆的钟



***The Paradigm Shift***

***Watch run with a Quartz Crystal***  
靠石英晶体走时的表



***Discovered in 1880*** 发现于1880年

***Seiko made 1<sup>st</sup> watch in 1969***  
1969年日本精工 (Seiko) 公司制造  
第一只石英表

# *History of Problem Solving in Soil Mechanics*

土力学中解决问题的发展历史

- ❑ **1930-1960 Era of closed-form solutions, graphical solutions and simple integration** 解析解，图解法和简单积分法时代
- ❑ **1960-1990 Era of development of digital computer hardware and computer solution software (as well as other software)** 计算机软硬件的发展与数值解法时代
- ❑ **1990-2000+ Era of a new generation of numerical modeling techniques and software capabilities with faster computers** 新一代数值模拟技术及软件，采用更强大的计算机

# *Geotechnical Engineering Changes in the 21<sup>st</sup> Century*

## 二十一世纪的岩土工程

- ❑ ***Saturated-Unsaturated Seepage analyses.***

饱和—非饱和渗流分析

- ❑ ***Contaminant Transport analyses for geo-environmental engineering.***

环境岩土工程中的污染物运移分析

- ❑ ***Stress-Deformation analysis for usage with:***

应力—变形分析，结合：

- ***Optimization Techniques (e.g. Dynamic Programming) for:*** 优化技术(如：动态规划)，应用于：

- ◆ ***Slope stability analyses*** 边坡稳定分析
- ◆ ***Lateral earth pressure analyses*** 侧向土压力分析
- ◆ ***Bearing capacity analyses*** 承载力分析

# *Geotechnical Engineering Changes in the 21<sup>st</sup> Century*

## 二十一世纪的岩土工程

- ❑ **Implementation of *Elasto-Plastic* models** 完善弹塑性模型
  - **Combining *stress-strain* and a *shear strength* model** 结合应力—应变关系和抗剪强度模型
- ❑ ***Geo-thermal* analyses** 地—热分析
  - ***Freeze-thaw analyses*** 冻融分析
  - ***Heat flow through saturated-unsaturated soil systems*** 饱和—非饱和土系统的热流
  - ***Soil-atmospheric models involving vapor flow*** 包括蒸气流的土壤—大气模型
- ❑ **Solving *Uncoupled* analyses** 非耦合分析
  - ***Importing pore-water pressures into slope stability analysis*** 将孔隙水压引入边坡稳定分析
  - ***Importing stresses into slope stability analyses*** 将应力引入边坡稳定分析

# *Geotechnical Engineering Changes in the 21<sup>st</sup> Century*

## 二十一世纪的岩土工程

### **Coupled: 耦合分析**

#### □ **Simultaneous solution of: 同时解决**

- **Seepage and stress-deformation analysis for**  
渗流与应力—变形耦合分析，应用于：
  - ◆ **Consolidation analysis** 固结分析
  - ◆ **Swelling clay analysis** 粘土的膨胀变形分析
  - ◆ **Collapsible soil analysis** 土的湿陷性分析
- **Seepage and Heat flow analysis (Soil-Atmospheric model)** 水的渗流与热流耦合分析(土壤—大气模型)
- **Seepage, thermal and stress analysis (Frost heave models)** 水的渗流，热流和应力耦合分析(冻胀模型)



# *The Problem We Face in Teaching Soil Mechanics*

## 土力学教学中遇到的问题

- ❑ ***Concepts and Principles of Soil Mechanics were defined in the 1930's and still form the context for most Soil Mechanics books***

概念和原理是二十世纪三十年代确立的，仍然被当今大多数土力学教材所遵循

- ❑ ***Consequently, a large gap exists between geotechnical engineering practice and what is taught in Soil Mechanics at universities***

导致了授课内容与工程实践的脱节

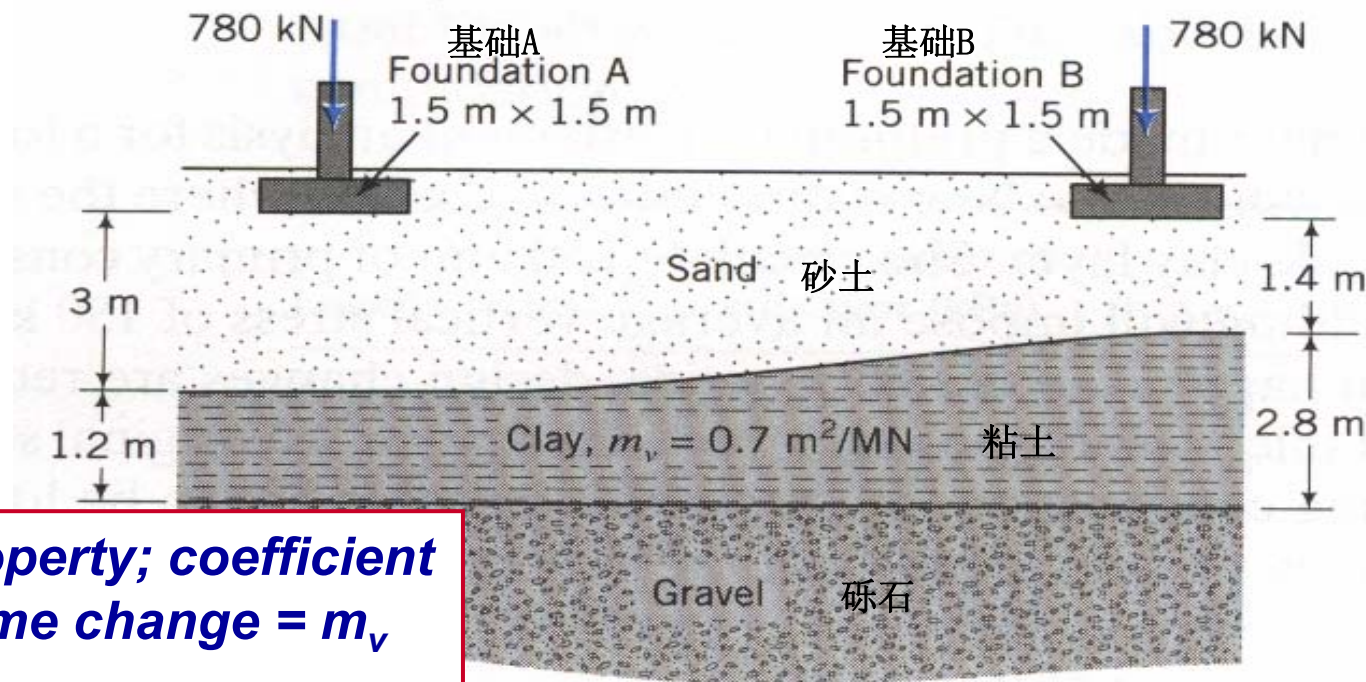
# Historical Categorization of Classic Soil Mechanics Problems

## 经典土力学问题的归类

### □ **Volume Change of soft compressible clays**

软土的体变

#### ● **Settlement Analyses** 沉降分析



**Soil property; coefficient of volume change =  $m_v$**

土的性质：体积变化率 =  $m_v$

# *Soil Mechanics Partial Differential Equations, PDEs*

## 土力学中的偏微分方程

- **All classic areas of soil mechanics can be viewed in terms of the solution of a *Partial Differential Equation*** 所有经典的土力学领域都可以看作求解偏微分方程
- ***Water flow through porous soils (Saturated or Unsaturated)*** 多孔介质的渗流(饱和或非饱和土)
- ***Stress analysis for slope stability, bearing capacity and earth pressure***  
应力分析，应用于边坡稳定，承载力和土压力问题
- ***Stress-Deformation volume change and distortion***  
应力—变形问题：体积变化和形变
  - ***Incremental elasticity*** 增量弹性模型
  - ***Elasto-plastic models*** 弹塑性模型

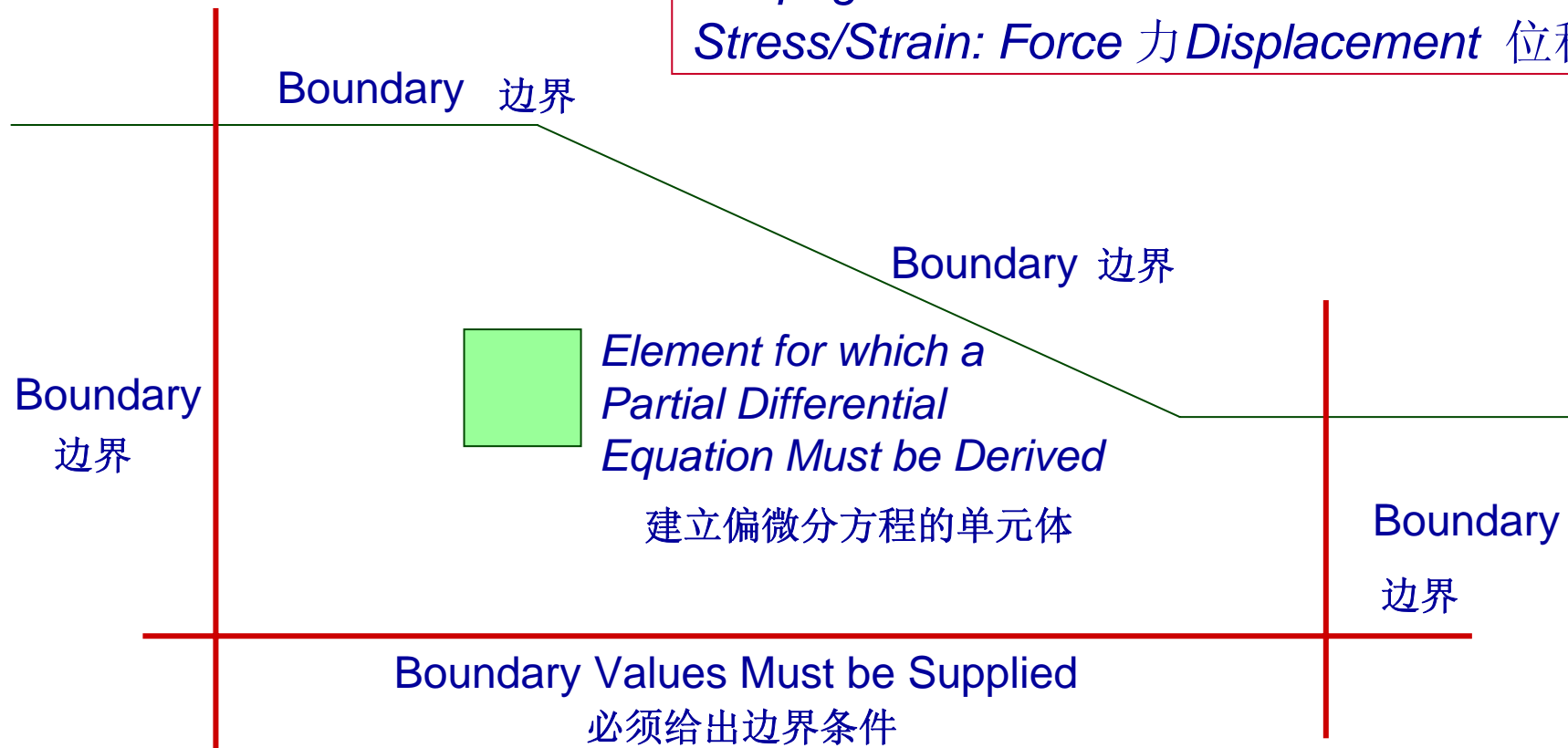
# Boundary Value Context for Geotechnical Engineering Problems

## 岩土工程中的边值问题

## Boundary Conditions

**Seepage: Flux 流量 Head (水) 头**

**Stress/Strain: Force 力 Displacement 位移**



## *Consider Flow Through Porous Media as an Example of Teaching from a PDE Base*

举例：如何以偏微分方程为基础，教授多孔介质的渗流

- **Start with picking an *REV* and defining what is meant by a “field”**

选取**REV** (**Representative Elementary Volume**), 即表征单元体积, 确定分析的“范围”

- **Derive the *Partial Differential Equation, PDE***  
列出偏微分方程

- **Explain the meaning of the *PDE* and the *Soil Properties*** 解释偏微分方程和土性的物理意义

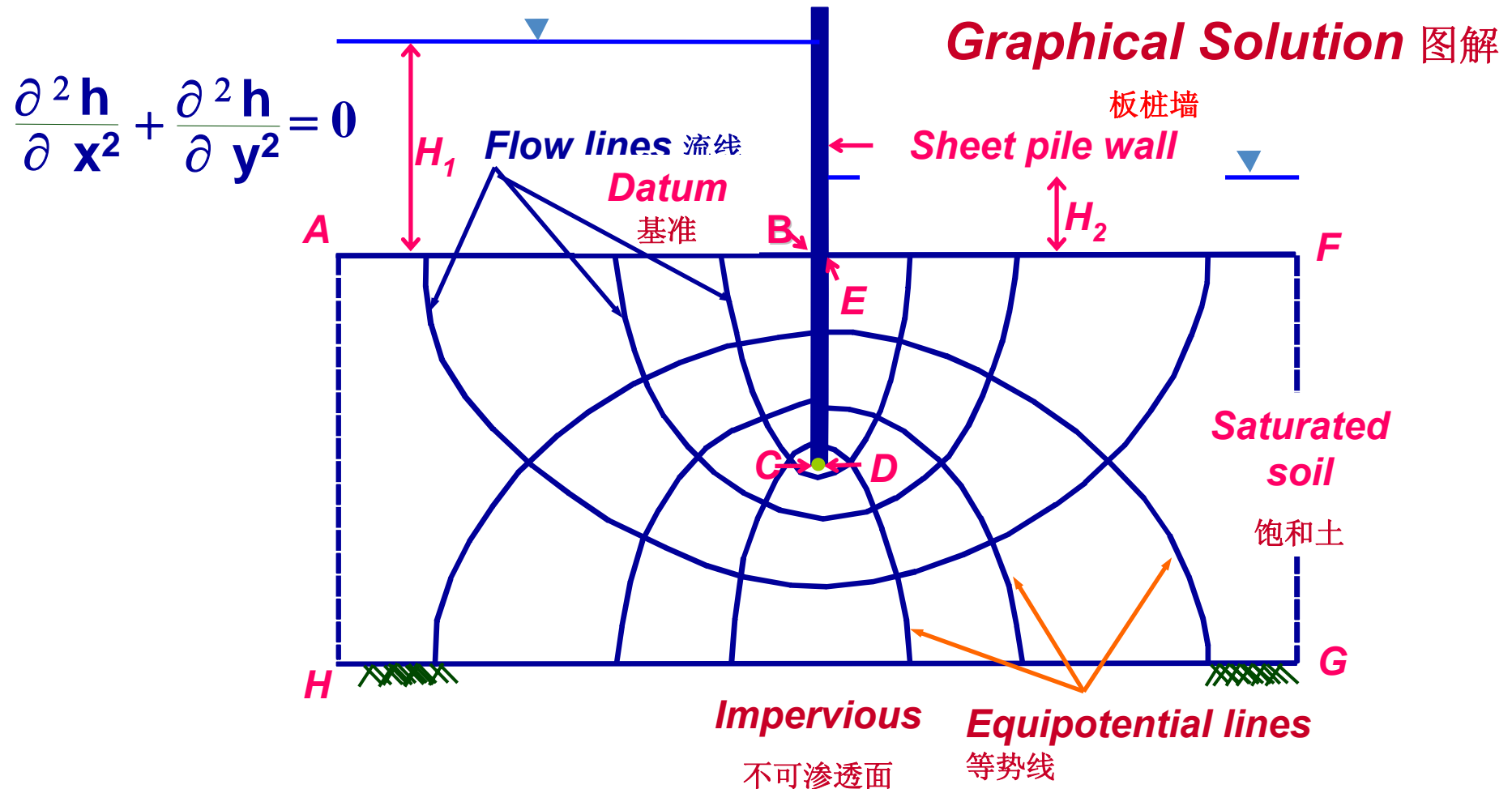
- **Solve & Interpret the Computer Results** 分析电算的结果



# *Steady State Seepage Flownets* 稳态渗流: 流网

- **Homogeneous, Isotropic, Saturated soil**
- 单一的饱和土

**Old Paradigm** 旧的模式



# Partial Differential Equation for Saturated-Unsaturated Water Flow Analysis

用偏微分方程进行饱和—非饱和渗流分析

**Head variable to be solved**

未知量：水头

$$k_x^w \frac{\partial^2 h}{\partial x^2} + \frac{\partial k_x^w}{\partial x} \frac{\partial h}{\partial x} + k_y^w \frac{\partial^2 h}{\partial y^2} + \frac{\partial k_y^w}{\partial y} \frac{\partial h}{\partial y} = -m_2^w \gamma_w \frac{\partial h}{\partial t}$$

**Water coefficient of permeability  
(function of soil suction)**

渗透系数（为吸力的函数）

**Water storage  
(function of soil suction)**

持水量（为吸力的函数）

**Time**

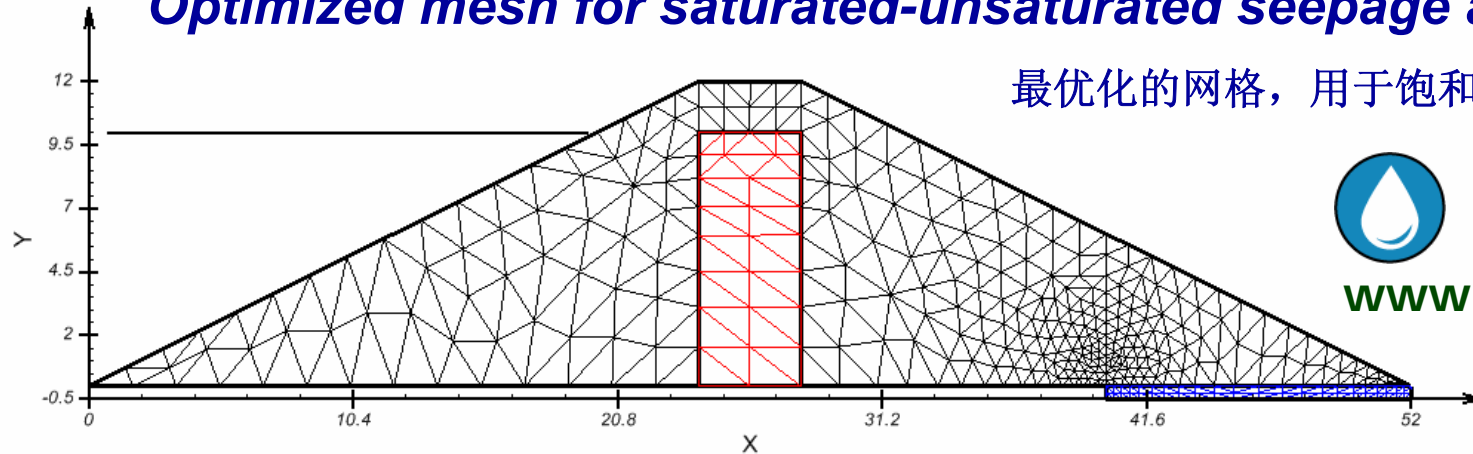
时间

# Two-dimensional seepage analysis through an earthfill dam with a clay core.

## 通过带粘土心墙的土坝的二维渗流分析

### Optimized mesh for saturated-unsaturated seepage analysis

最优化的网格，用于饱和一非饱和渗流分析

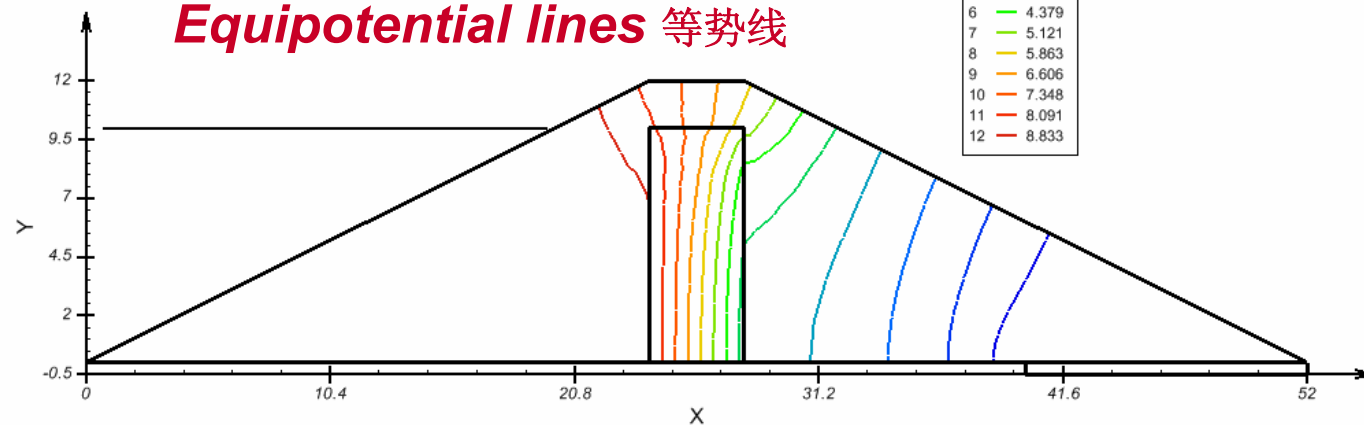


SVFLUX

[www.soilvision.com](http://www.soilvision.com)

Thieu and Fredlund, 1998

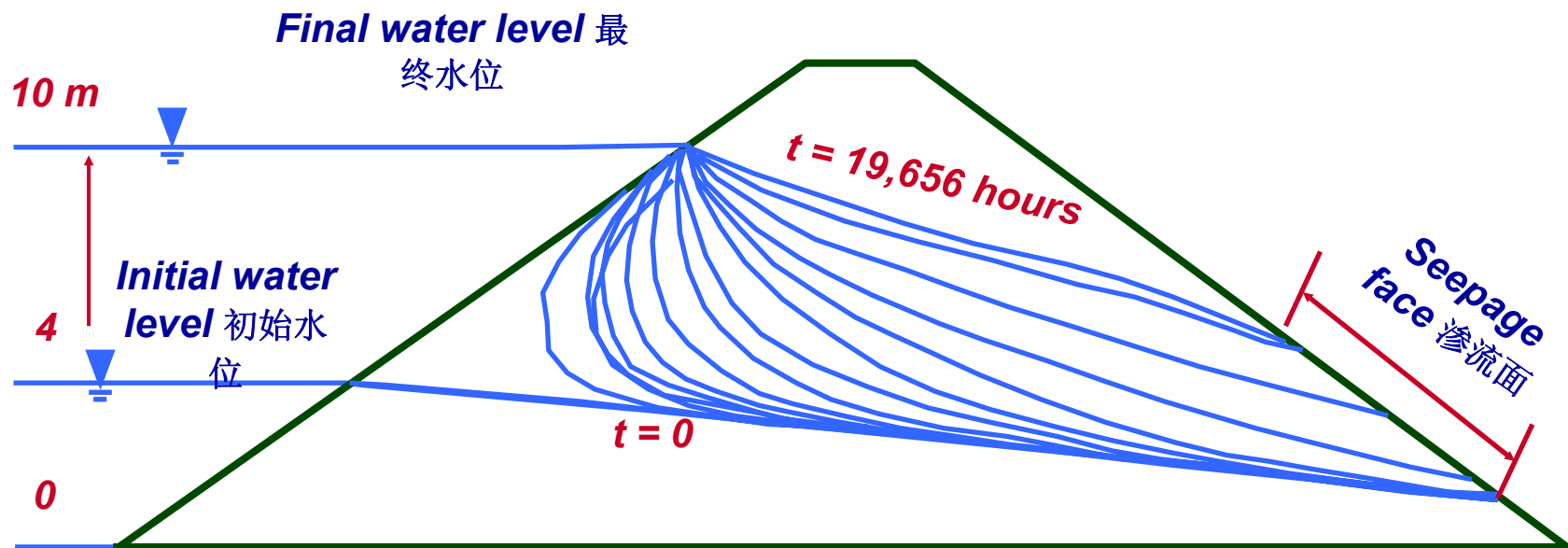
### Equipotential lines 等势线



# Transient Seepage Analysis Saturated-Unsaturated Soil Systems

## 饱和—非饱和瞬态渗流分析

- ❑ **Changing zero pressure isobar with time**  
零等压线随时间变化
- ❑ **Total elapsed time, transient is 19,658 h**  
总历时为19,658小时



# Introduction to Unsaturated Soils

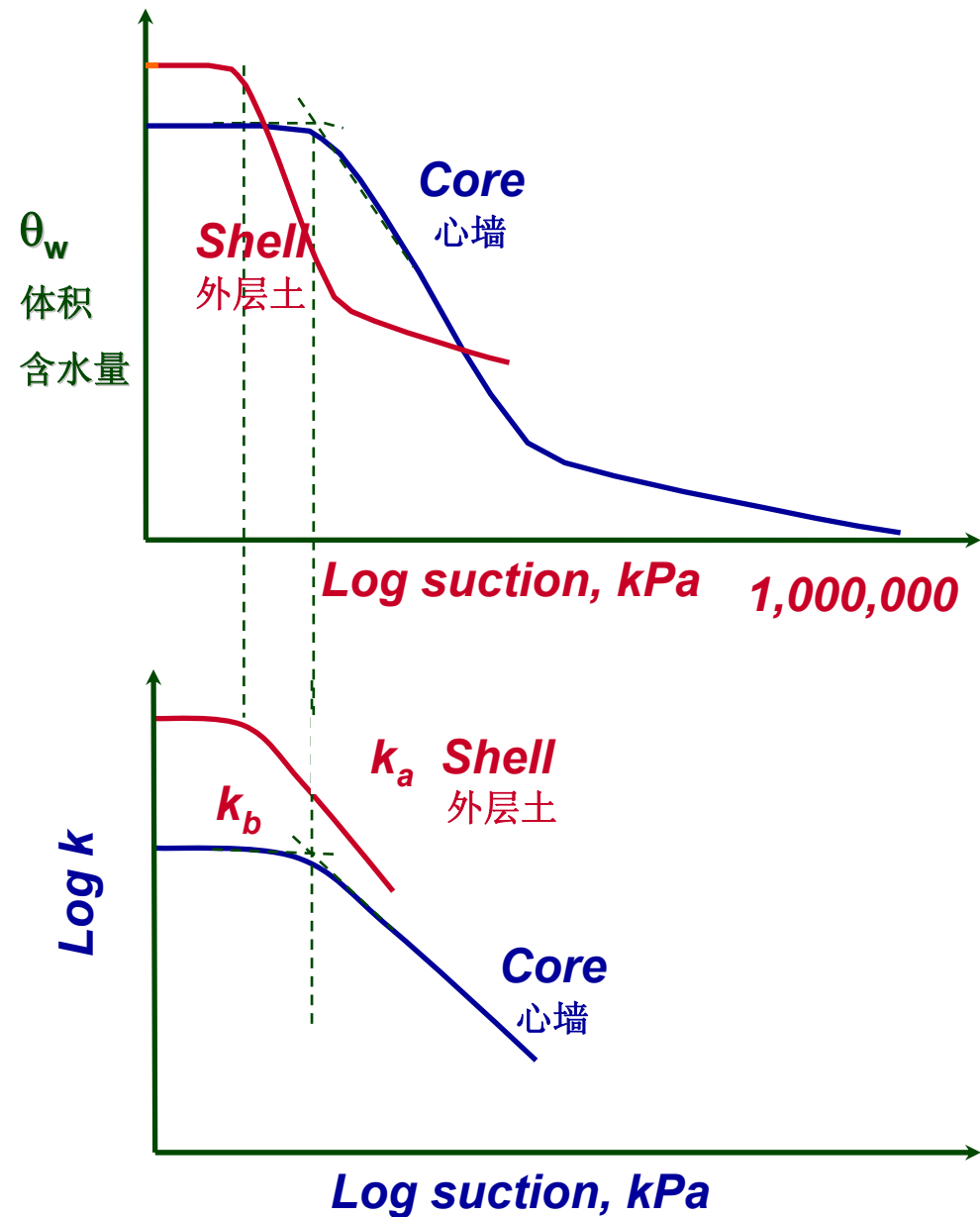
非饱和土介绍

*Permeability Function  
indirectly determined  
from the SWCC*

渗透性函数常通过SWCC,  
即土水特征曲线间接确定

**Relationship of the  
SWCC to the  
Permeability Function**

SWCC与渗透性函数的关系





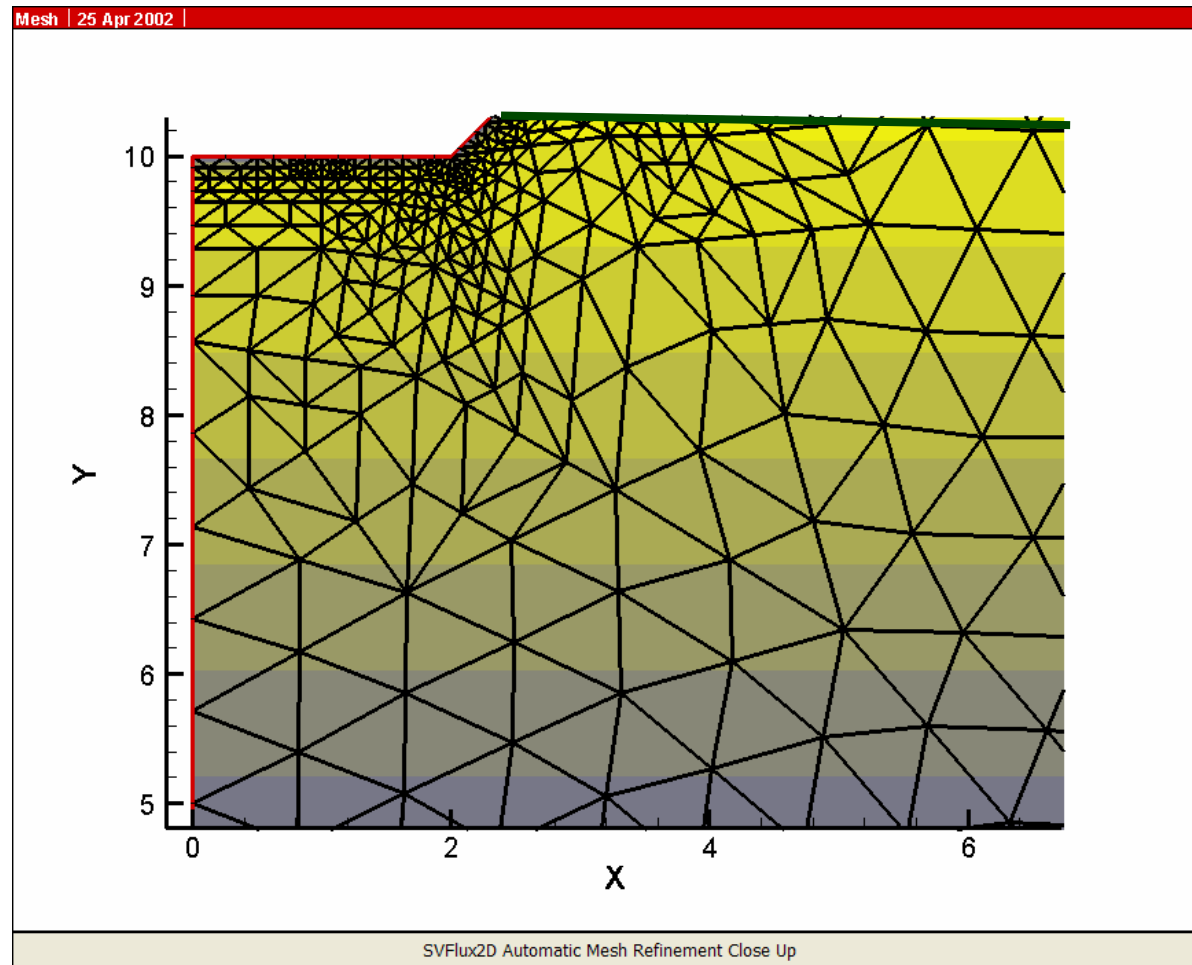
# *Convergence of Nonlinear Partial Differential Equations*

## 非线性偏微分方程的收敛

- ***Convergence is the single most pressing problem facing modelers*** 收敛是模拟软件面临的最迫切的问题
- ***Most successful solutions have involved Adaptive Grid Refinement methods, AGR (Oden, 1989; Yeh, 2000)*** 大多数成功的解法采用了自适应网格细化技术，即**AGR**
- ***Mesh is dynamically upgraded during the solution based on error estimates*** 基于误差估测，网格可在求解过程中动态地升级

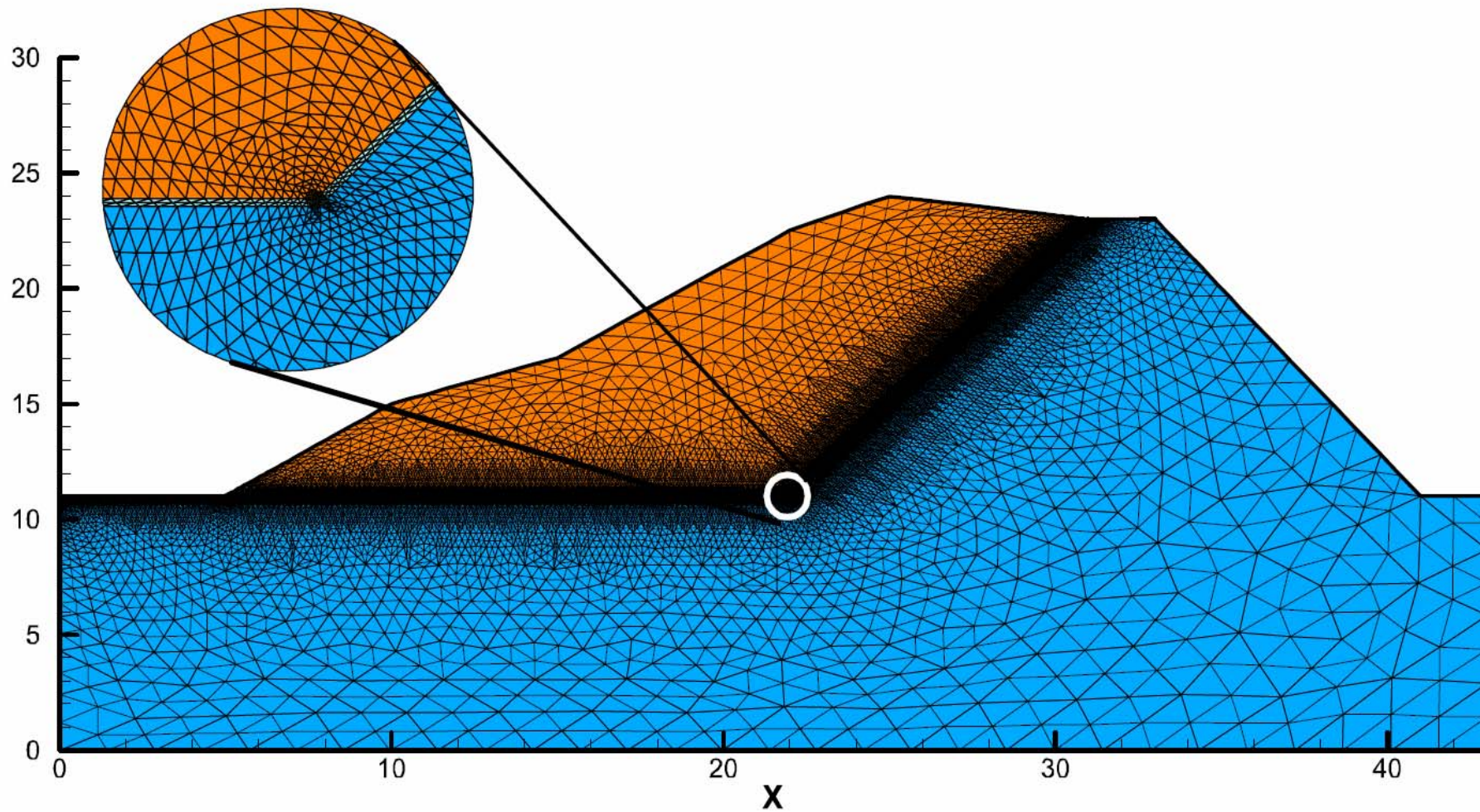
# *Contaminant Transport with Automatic Mesh Refinement*

网格自动细化在污染物扩散中应用



# *Retainment Dyke with an Internal Geomembrane*

中间含土工膜的堤坝的网格细化



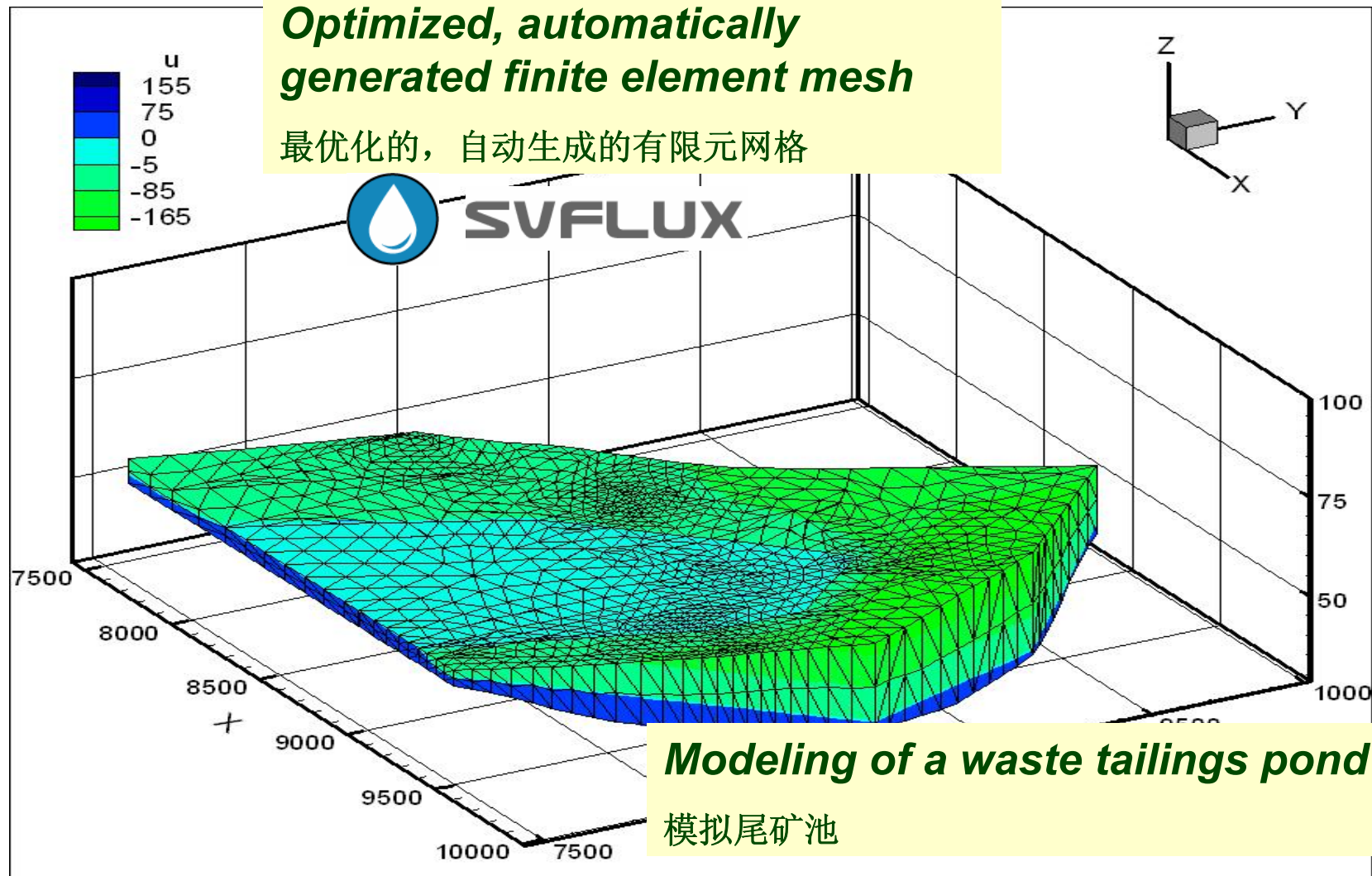


*Problem illustrating the solution of a 3-dimensional,  
saturated-unsaturated seepage PDE*

举例：解决三维饱和—非饱和渗流偏微分方程

**Optimized, automatically  
generated finite element mesh**

最优化的，自动生成的有限元网格



**Modeling of a waste tailings pond**

模拟尾矿池

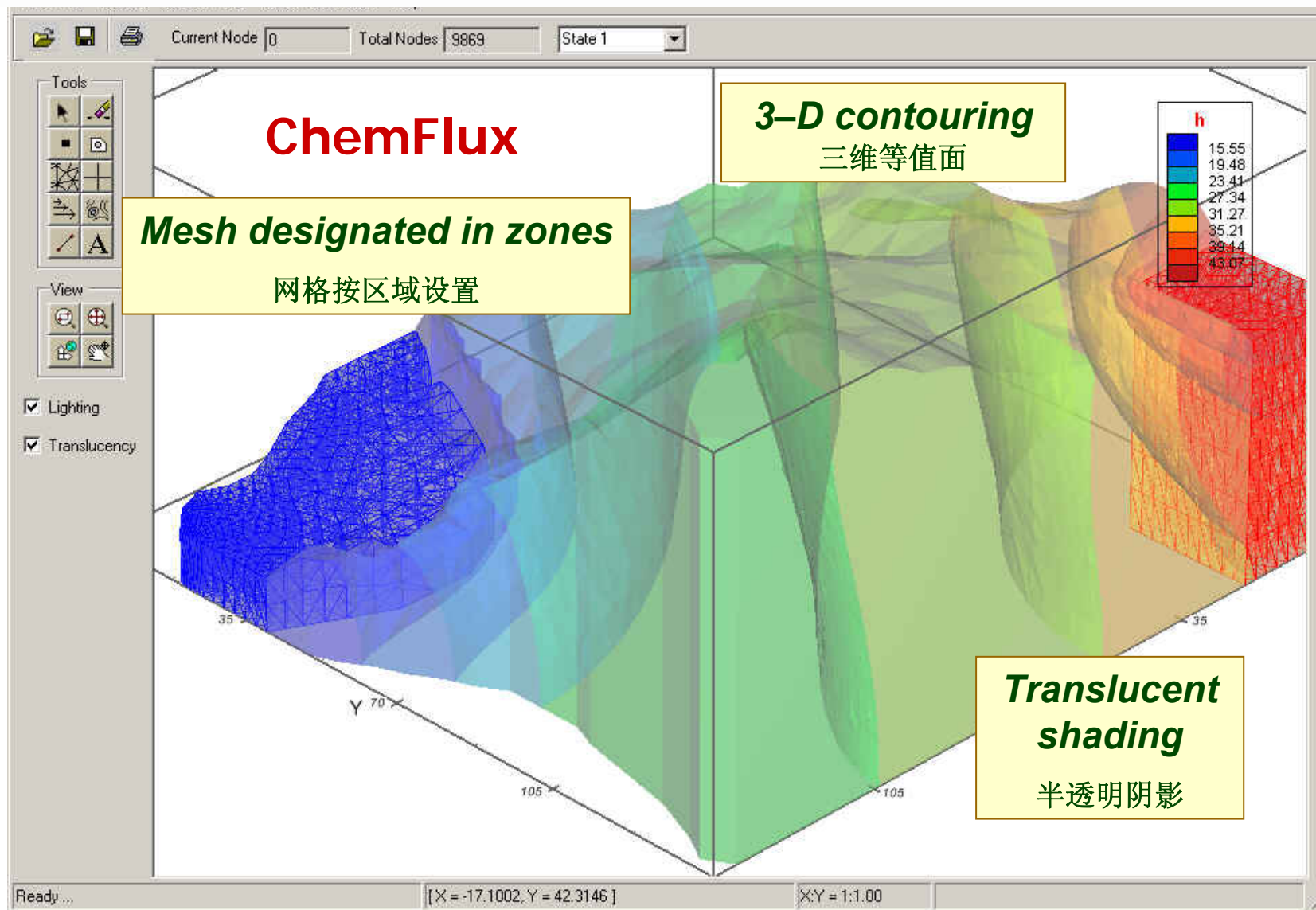
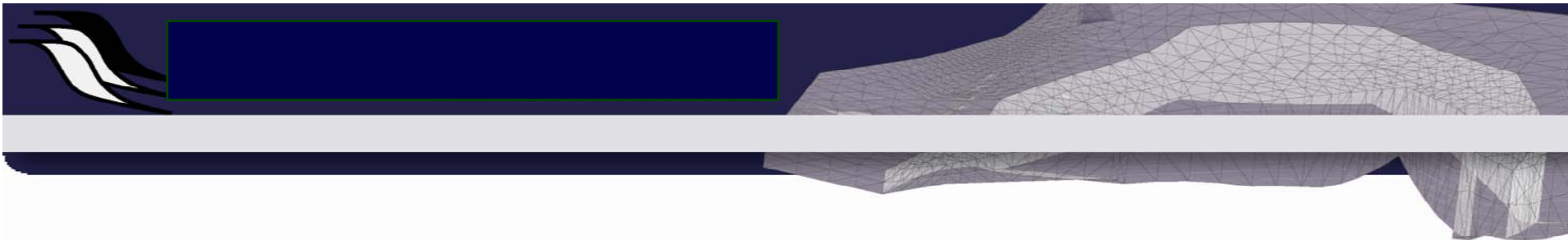
# **Typical Subjects Covered in a Conventional Soil Mechanics Book** (*Soil Mechanics & Foundations* by M. Budhu) 常规的土力学书中涵盖的典型问题

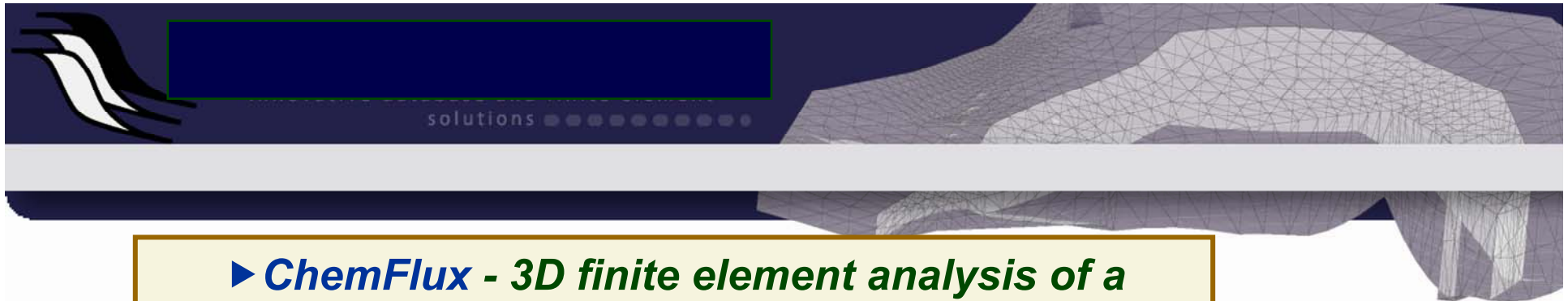
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- *Definition of Head and Darcy's Law* 定义水头和达西定律
  - *Estimation of the Saturated Permeability* 估测饱和渗透系数
  - *Measurement of Coefficient of Permeability* 测量渗透系数
  - *Flow Parallel and Perpendicular to Soil Layers* 平行和垂直于土层方向的渗流
  - *Criteria for Sketching Flow Nets* 绘制流网的原则
  - *Flow Nets for Isotropic Soils* 各向同性土的流网绘制
  - *Flow Through Anisotropic Soils* 各向异性土中的渗流
  - *Flow Rates* 渗流速率
  - *Hydraulic Gradients* 水力梯度
  - *Critical Hydraulic Gradients* 临界水力梯度
  - *Uplift Forces* 浮托力
  - *Flow Through Earth Dams* 土坝的渗流
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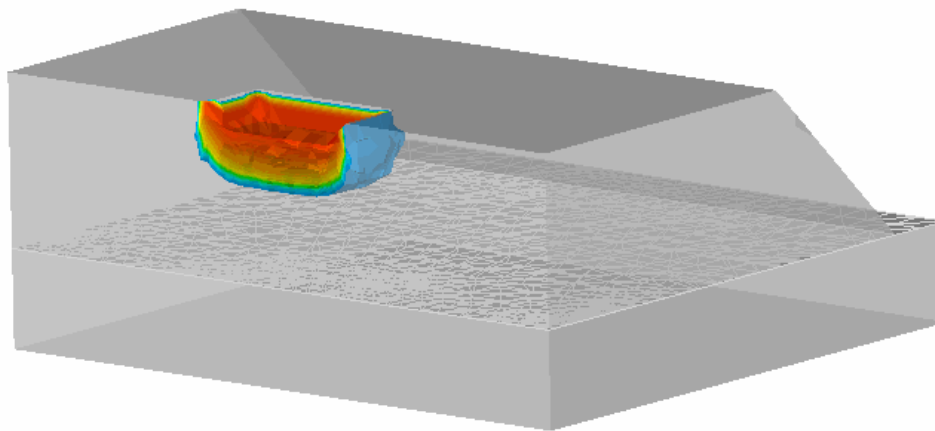






► ***ChemFlux - 3D finite element analysis of a contaminant transport problem (animated)***

污染物运移问题的三维有限元分析（动画模拟）



# *Thermal Analysis for Saturated- Unsaturated Soil Systems*

饱和—非饱和系统的热分析

- ❑ ***Heat flow partial differential equations are similar to water flow except for the Latent heat associated with:***

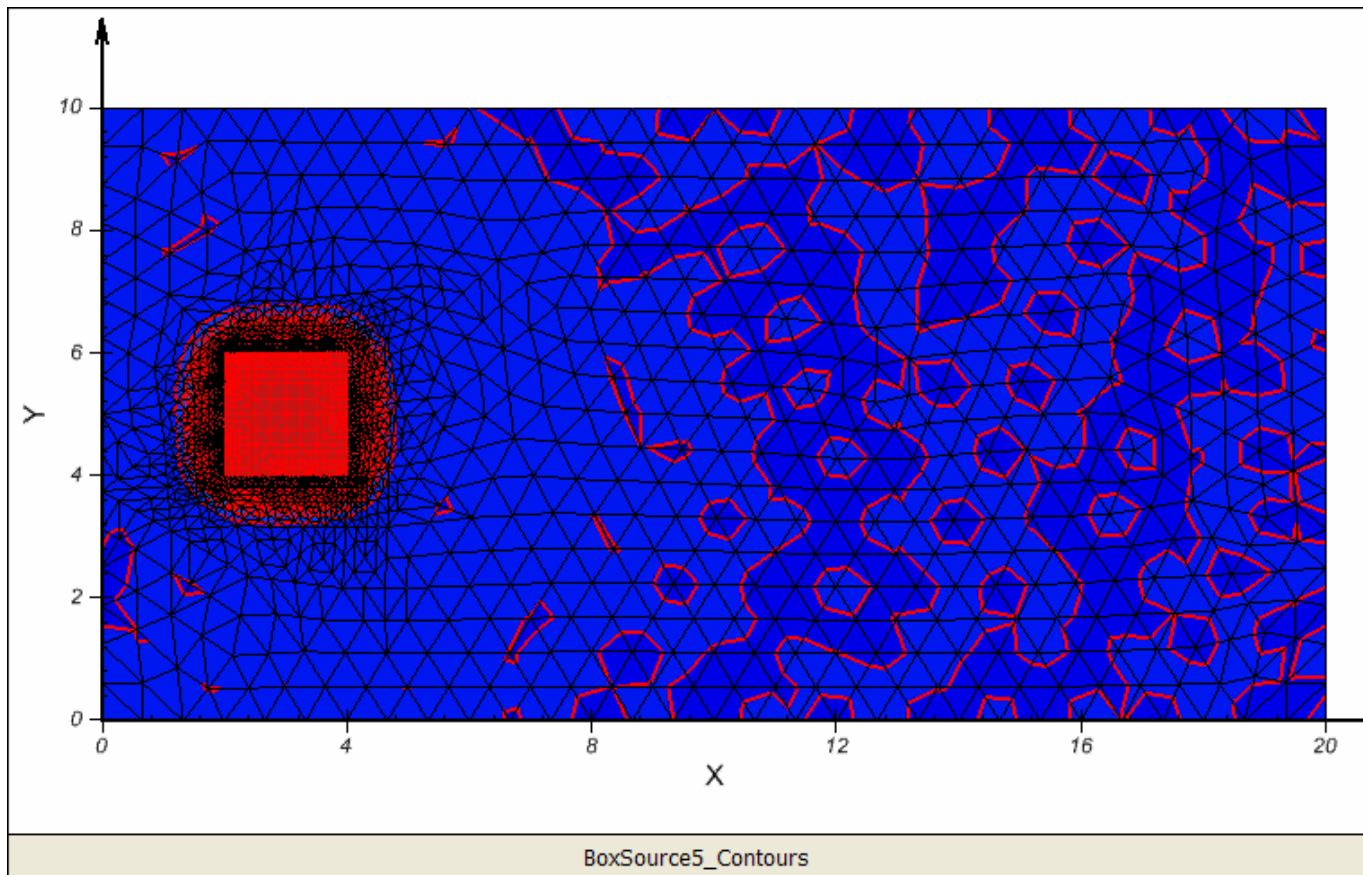
热流偏微分方程与水流相似，除了以下两种相态变化：

- ***freezing and thawing*** 冻融
- ***vaporization*** 蒸发

- ❑ ***Thermal soil properties are a function of the soil-water characteristic curve , SWCC*** 土的热性质是土水特征曲线，即SWCC的函数

► **SVHeat** - 2D finite element analysis of a problem with  
*extremely steep thermal gradients*

热梯度极其陡的条件下的二维有限元分析



# Partial Differential Equation for Saturated-Unsaturated Stress-Deformation Analysis

## 饱和—非饱和土应力—变形分析的偏微分方程

$$\frac{\partial}{\partial x} \left[ D_{11} \frac{\partial u}{\partial x} + D_{12} \frac{\partial v}{\partial y} \right] + \frac{\partial}{\partial y} \left[ D_{44} \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) \right] = 0 \quad \text{X-}$$

$$\frac{\partial}{\partial x} \left[ D_{44} \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) \right] + \frac{\partial}{\partial y} \left[ D_{12} \frac{\partial u}{\partial x} + D_{11} \frac{\partial v}{\partial y} \right] + \gamma_t = 0 \quad \text{Y-}$$

**$D_{11}$ ,  $D_{12}$ ,  $D_{44}$  = Combination of  $E$  and  $\mu$  which are function of soil suction and net total stresses**

结合 $E$ 和 $\mu$ ，二者是吸力和净正应力的函数

**Stress-deformation analyses have a degrees of freedom in each of the Cartesian coordinate directions**

应力—变形分析在每个笛卡儿坐标下都有一个自由度



## SVSolid

**Hooke's Law** 胡克定律

**Linear Elastic** 线弹性

**Non-linear Elastic** 非线性弹性

**Anisotropic Linear Elastic**

各向异性线弹性

**Hyperbolic** 双曲线形应力应变曲线

**Mohr-Coulomb Failure Criteria**

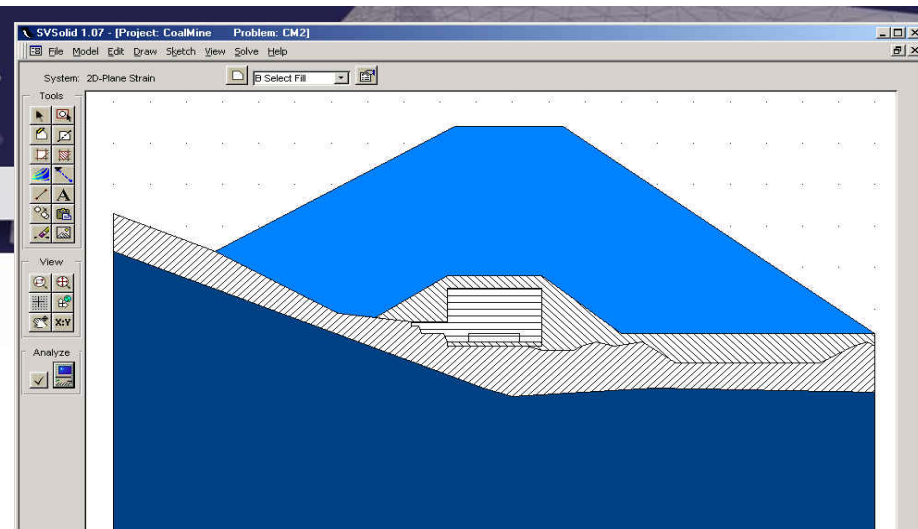
摩尔-库仑破坏准则

### *Analysis Types* 分析形式

**2-D Plane Strain** 二维平面应变

**Axisymmetric** 轴对称

**3-D** 三维



### *Behavior - Set By Soil Region*

土性在“区域”中定义

**Effective or total stress parameters**

有效应力或总应力参量

**Drained or undrained analysis**

排水或不排水的情况

**Skempton A and B parameters to calculate pore-water pressure**

斯肯普顿A, B值, 用以计算孔隙水压

**Body loads applied for any particular soil region**

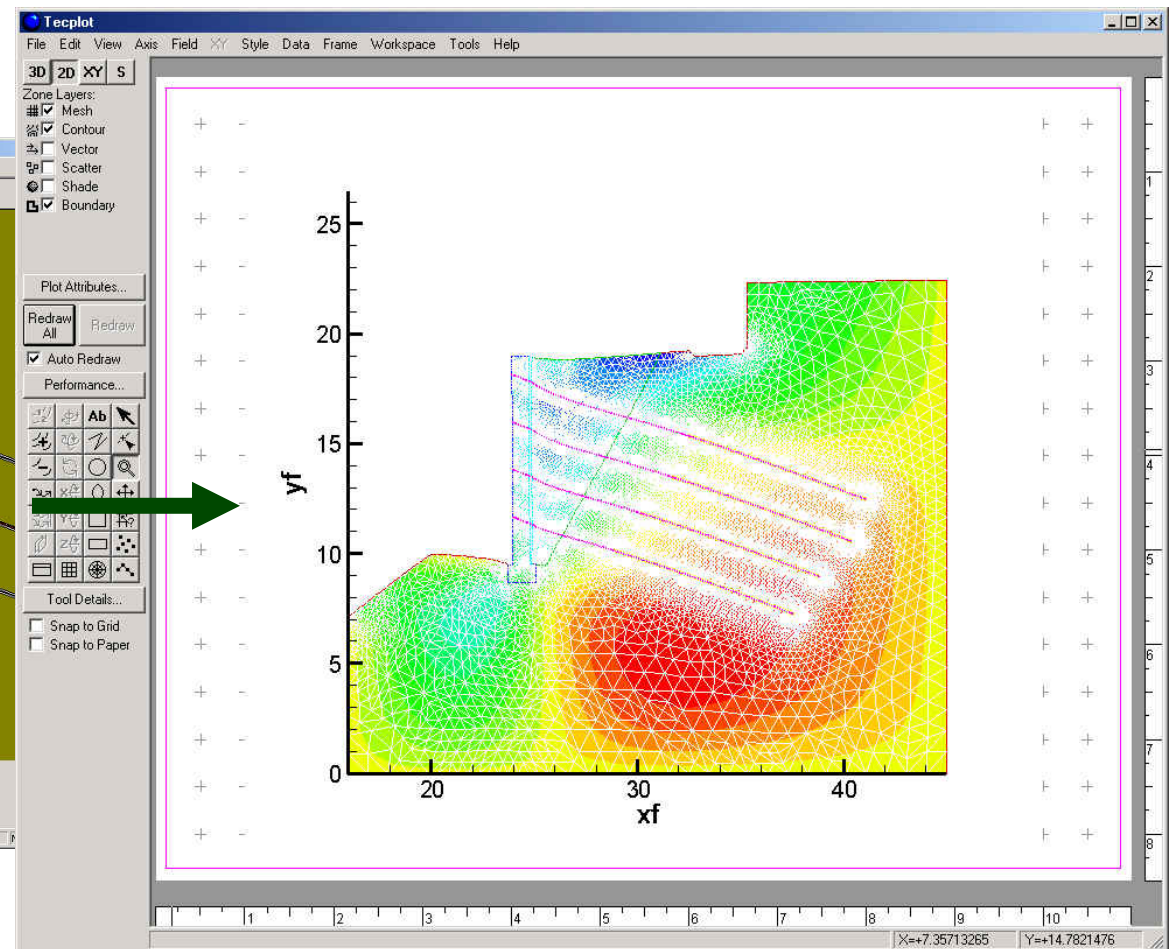
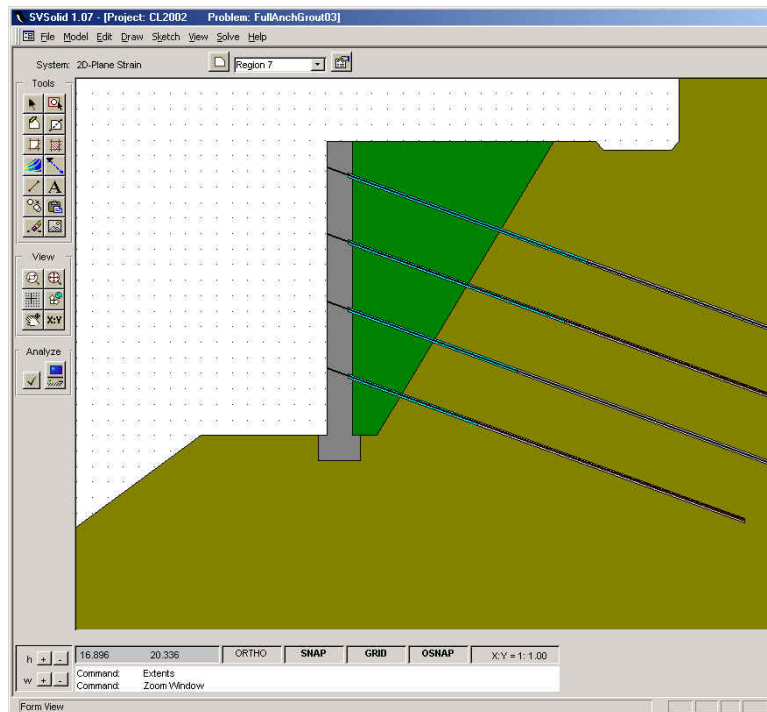
特定区域所受的体积载荷



# SVSolid

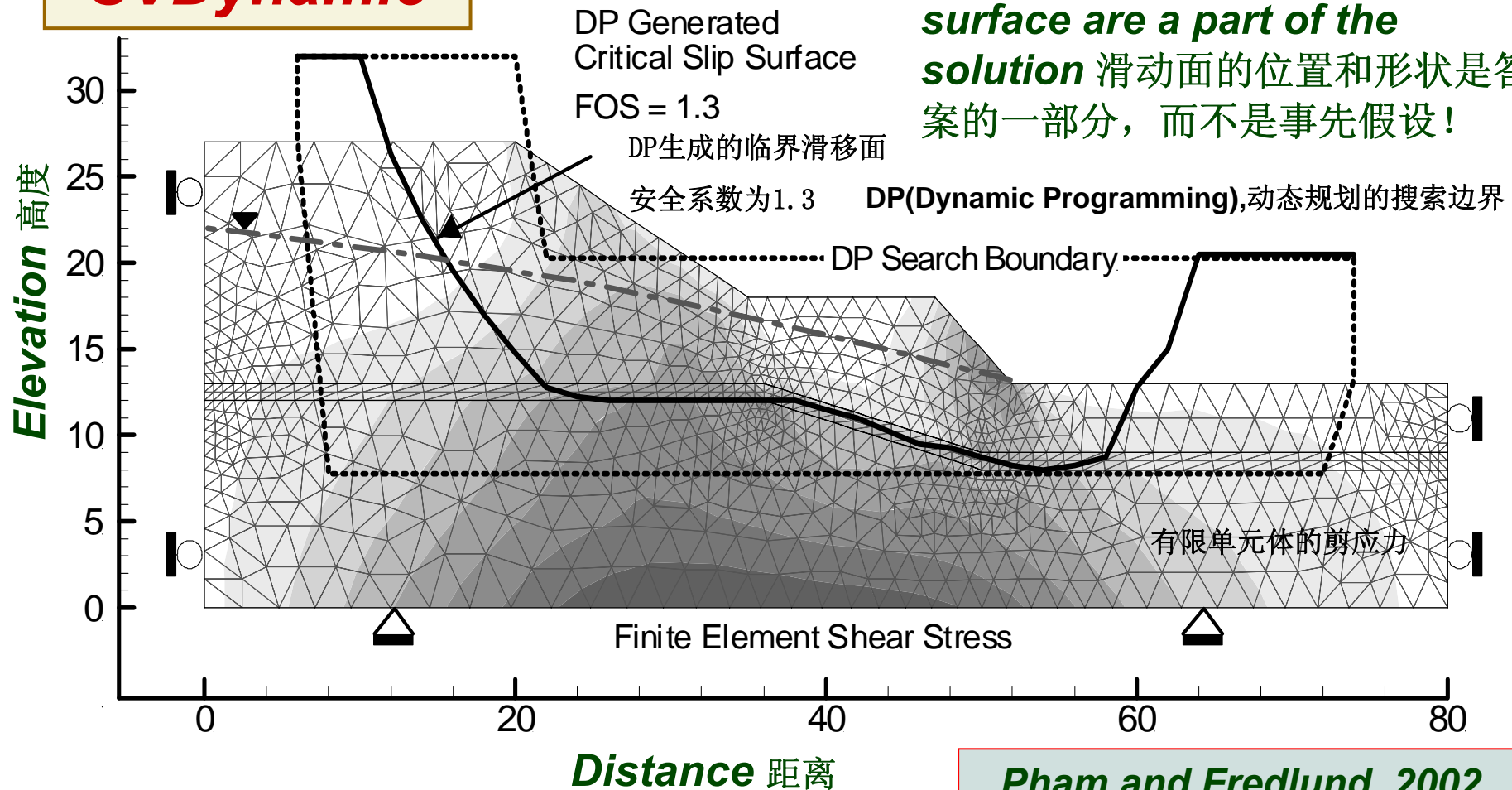
*Representation of extremely fine features* 显示细致入微

*Complex structures*



*Stress analysis can be combined with the Dynamic Programming to compute the factor of safety*  
应力分析结合动态规划，计算安全系数

**SVDynamic**



**Pham and Fredlund, 2002**

# Prediction of Heave or Collapse of a Soil 预测土的隆胀与湿陷

**Must consider effects of:** 需要考虑

**-Nonlinearity** 非线性

**-Coupling** 耦合作用

**Slab-on-ground**

$\zeta$

**Coupled** 耦合  
**Uncoupled** 非耦合  
**Pseudo-coupled** 准耦合

**Saturated-Unsaturated  
Seepage Model**

饱和—非饱和渗流模型

**Computes changes in suction**

计算基质吸力的变化

**Saturated-Unsaturated  
Stress-Deformation Model**

饱和—非饱和应力—变形模型

**Computes deformations**

计算变形

# Consider Edge Lift for a Flexible Impervious Cover

考虑不透水柔性覆盖层的边界上抬

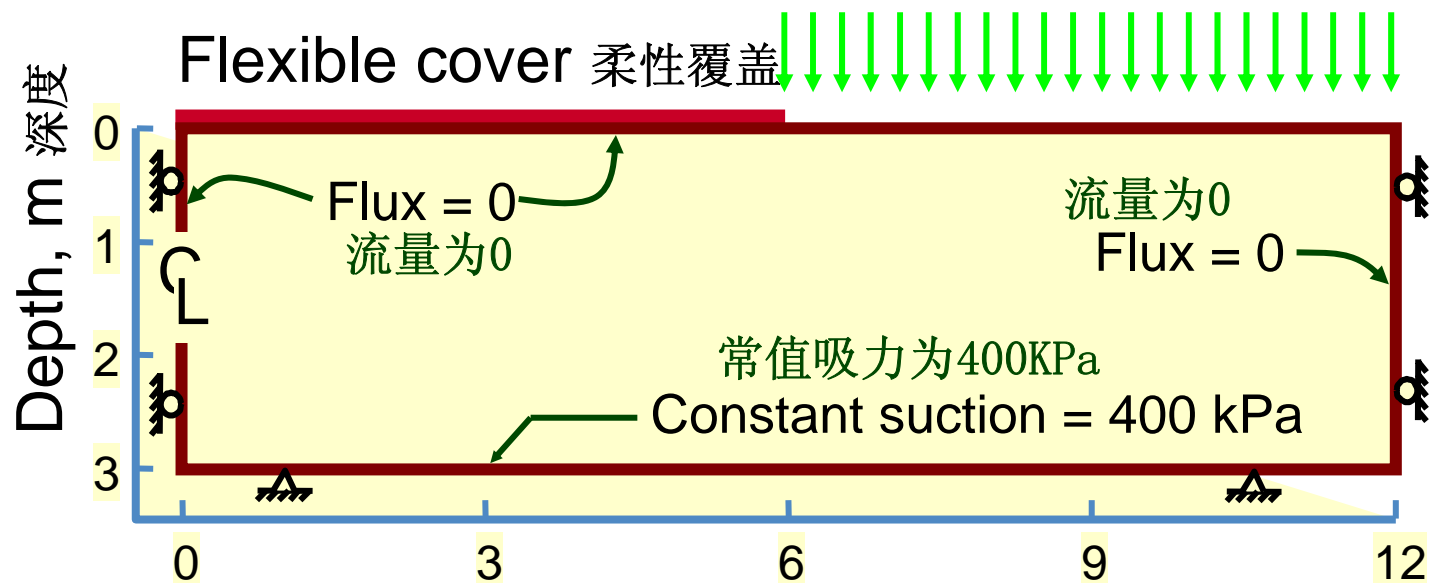
**Boundary conditions and initial conditions must be specified both seepage and stress-deformation**

进行渗流和应力—变形分析，必须给出边值和初值条件



SVFLUX

Infiltration,  $q$  入渗



Distance from centre of cover or slab, m

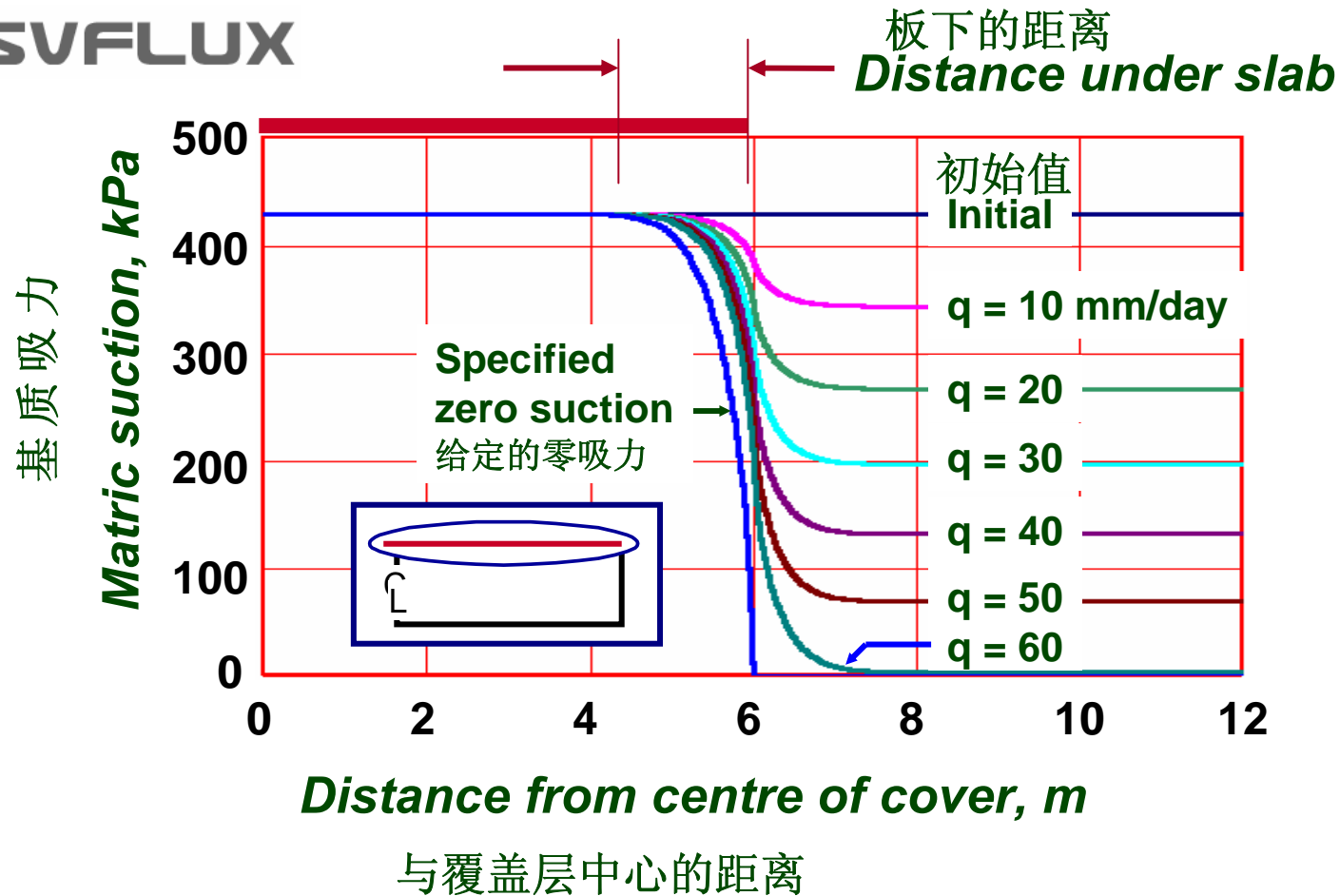
与覆盖层或板中心的距离

# Matric Suction at Ground Surface after One Day of Infiltration for Various Infiltration Rates

不同入渗速率下，一天后地表的基质吸力

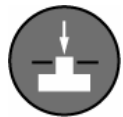


SVFLUX

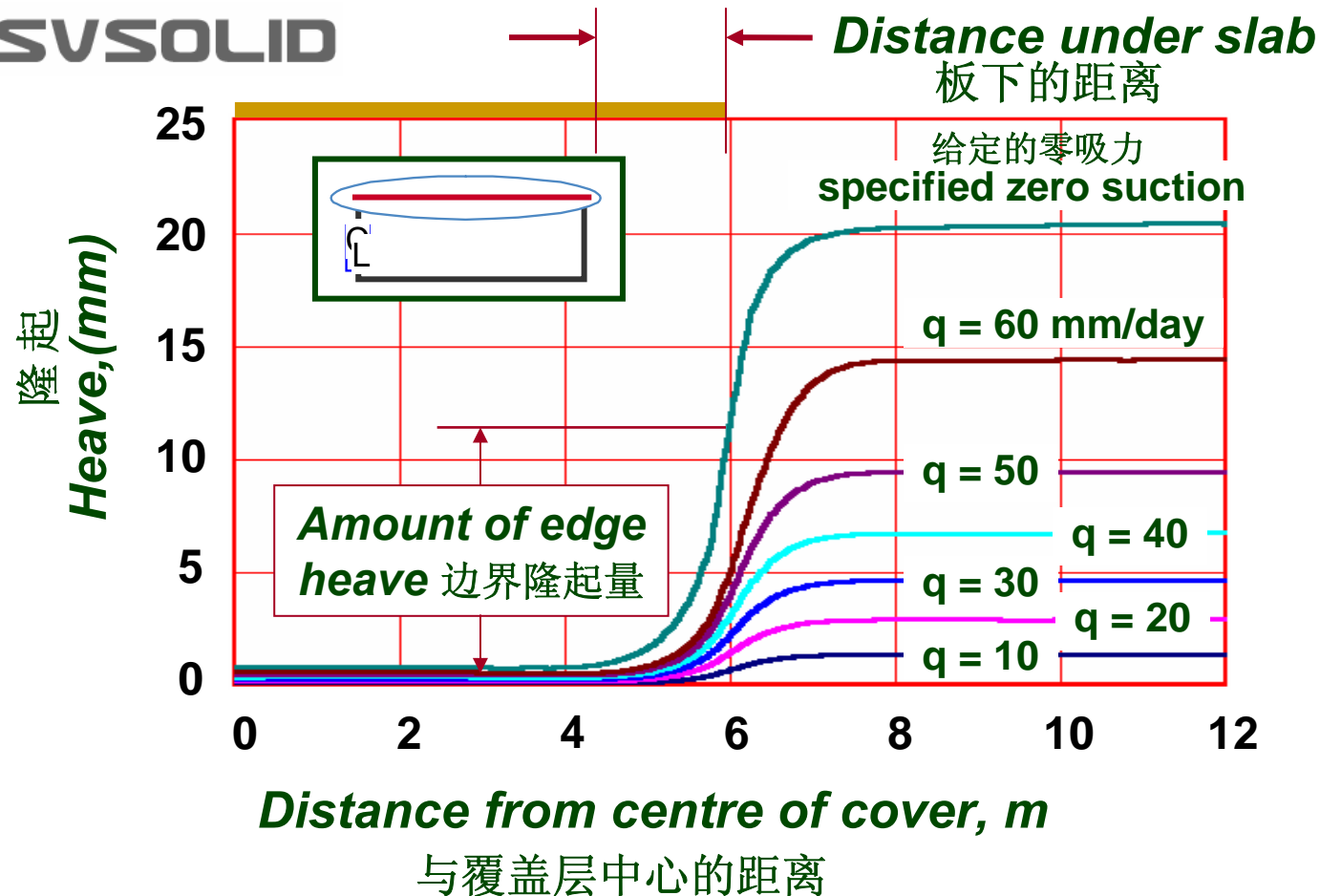


# Vertical Displacements at Ground Surface after One Day of Infiltration

入渗一天后，地表的竖向位移



SVSOLID





# *Observations on Teaching Soil Mechanics from a PDE Basis*

基于偏微分方程，讲授土力学的一些观察心得

- ***Saturated-unsaturated soil systems can be described in terms of a variety of nonlinear partial differential equations*** 饱和-非饱和土系统可以通过一系列非线性偏微分方程描述

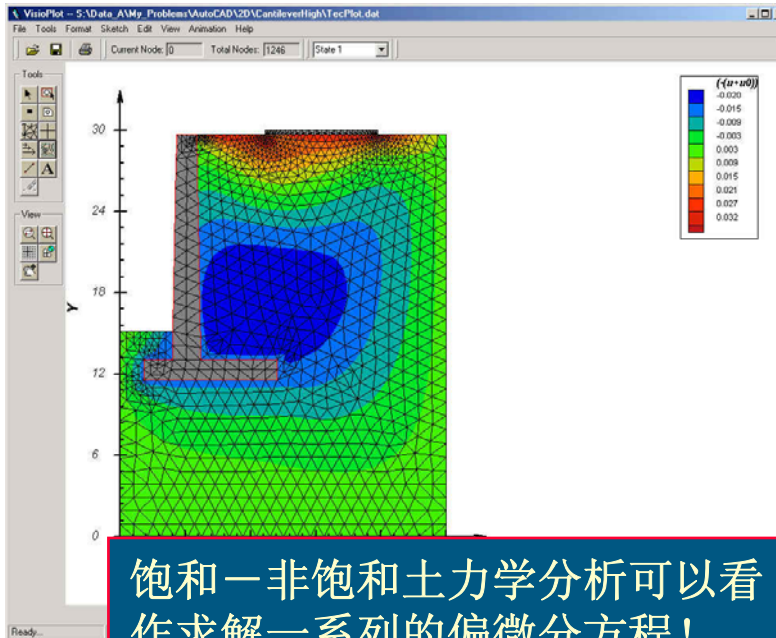
- ***Unsaturated soil property functions can be related to the soil-water characteristic curve***

非饱和土的土性参数可与其土水特征曲线相联系

- ***Partial differential equations are derivable for:***

偏微分方程可以这样得到

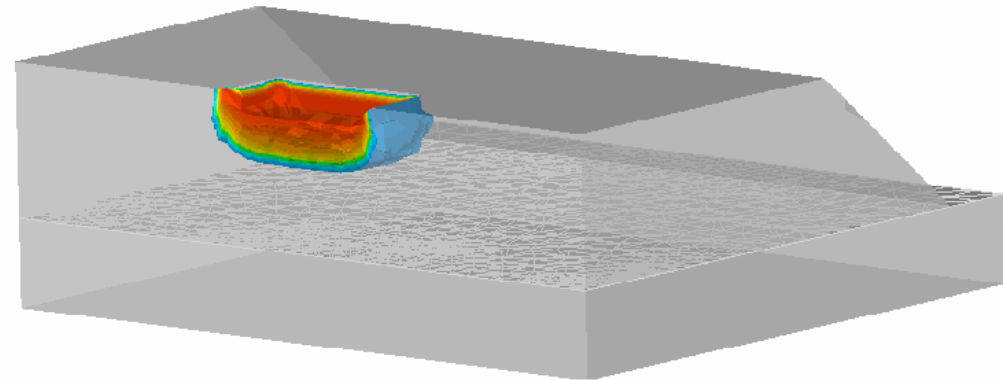
- ***one, two and three-dimensional problems*** 一维，二维和三维问题
- ***water flow*** 水的流动
- ***Stress-deformation analysis*** 应力-变形分析
- ***contaminant transport*** 污染物运移
- ***thermal analysis involving evaporation or freeze-thaw*** 包含蒸发或冻融的热分析
- ***vapor flow and air flow*** 蒸汽流和空气流



饱和-非饱和土力学分析可以看作求解一系列的偏微分方程！

## **Conclusion:**

*Geotechnical engineering analyses for  
Saturated-Unsaturated Soil Mechanics  
can indeed be viewed as the Solution of a  
Series of Partial Differential Equations*  
*Delwyn G. Fredlund*



D1-3DPosterProblem